Bathwick St Mary Progression and Calculation Document—Overview

Year Six

The following documents are used to provide us with a long term planning structure for teaching an learning over the year. We use the combination alongside our own teacher judgement and remain flexible for several reasons, taking into account:

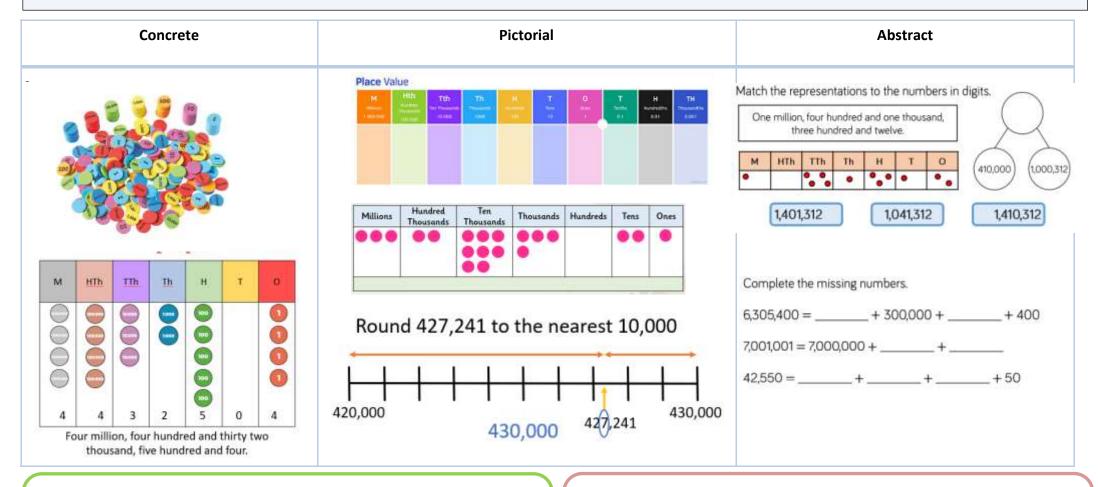
• The pace of the children's understanding in line with our whole class teaching for mastery approach

		Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12
	Autumn		r: Place lue	Number: Addition, Subtraction, Multiplication and Division			Fractions			Geometry: Position and Direction			
	Spring	Number: Decimals			nber: ntages Number: Algebra		Measurement: Converting Units	Perimet	rement: er, Area olume	Numbe	er: Ratio	Statistics	
_	Summer	Geometry: Properties of Shapes SATs week Consolidation of all areas		Investig	ations and	d preparat	tion for KS3	maths.					

Progression and Calculation Document— Place Value Year Six

NC Learning Objectives:

- Read, write, order and compare numbers up to 10,000,000 and determine the value of each digit.
- Round any whole number to a required degree of accuracy.
- Use negative numbers in context, and calculate intervals across zero.
- Solve number and practical problems that involve all of the above.



Key Vocabulary:

Digit Ones Thousands Millions

Value Tens Tens of Thousands Hundreds

STEM Sentences:

Why do we round up when the following digit is 5 or above?
Why is the zero in a number important when representing large numbers?
If one million is the whole, what could the parts be?

Place in here any additional Knowledge you think appropriate in each element having reviewed the knowledge organiser for your year group for each of the strands of maths.

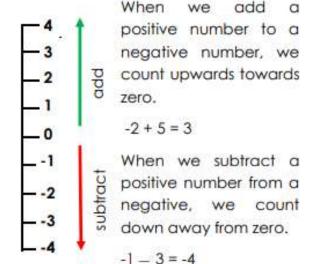
Negative Numbers

If you count backwards from zero, you reach negative numbers.

Positive numbers are any numbers more than zero e.g. 1, 2, 3, 4, 5.

Negative numbers are any numbers less than zero e.g. -1, -2, -3, -4, -5.

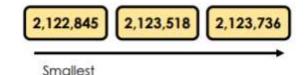




Ordering Numbers

When we put numbers in order, we need to compare the value of their digits.

First, look at the millions digits in each number. Each number has the same digit in the millions place so you then keep comparing digits of the same place value until you find ones that are different. The thousands digits are different so that tells us that 2,122,845 is the smallest number because it has a 2 in the thousands place. Looking at the hundreds digits, we can see that 2,123,518 is the next smallest.



Rounding

When rounding, you first need to identify which digit will tell you whether to round up or down.

- To round a number to the nearest 10, you should look at the ones digit.
- To round a number to the nearest 100, you should look at the tens digit.
- To round a number to the nearest 1000, you should look at the <u>hundreds</u> digit.
- To round a number to the nearest 10,000, you should look at the thousands digit.
- To round a number to the nearest 100,000, you should look at the ten thousands digit.
- To round a number to the nearest 1,000,000, you should look at the <u>hundred thousands</u> digit.

527,356 to the **nearest 10** is 527,360 527,356 to the **nearest 100** is 527,400 527,356 to the **nearest 1000** is 527,000

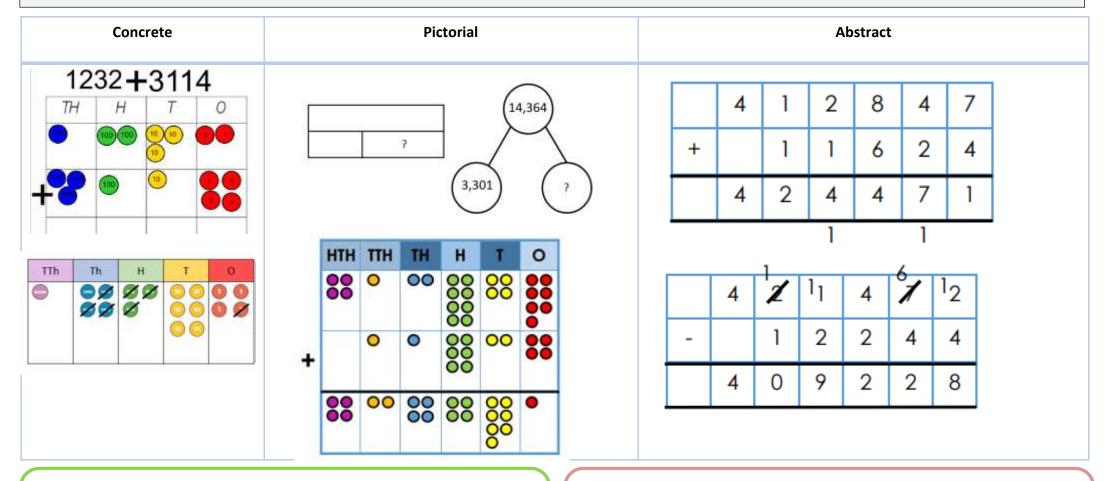




527,356 to the **nearest 10,000** is 530,000 527,356 to the **nearest 100,000** is 500,000 527,356 to the **nearest 1,000,000** is 1,000,000

NC Learning Objectives:

- Solve addition and subtraction multi step problems in contexts, deciding which operations and methods to use and why.
- Perform mental calculations, including with mixed operations and large numbers.
- Use their knowledge of the order of operations to carry out calculations involving the four operations.
- Solve problems involving addition, subtraction, multiplication and division.



Key Vocabulary:

Addition Carrying Sum Less than

Subtraction Column Difference

STEM Sentences:

Why is it important that we start subtracting the smallest place value first? Does it matter that the two numbers don't have the same amount of digits? What is the inverse of addition? What is the inverse of subtraction?

Place in here any additional Knowledge you think appropriate in each element having reviewed the knowledge organiser for your year group for each of the strands of maths.

Inverse Operations

Inverse means opposite. The opposite of addition is subtraction and therefore the opposite of subtraction is addition. Using an inverse operation is a useful way of checking your answer.



I have calculated that 214,257 -15,483 = 198,774. How can I check my answer?

To check the answer to your subtraction, you can use the inverse, which is addition. If we add 15,483 to your answer of 198,774 it should total 214,257 - your original number. If it does, you have calculated correctly.



Find the missing digits. What do you notice?

	5	2	2	4	7	?
+	3	?	5	9	0	4
	9	0	?	3	?	2

Progression and Calculation Document — Multiplication and division Year Six

NC Learning Objectives:

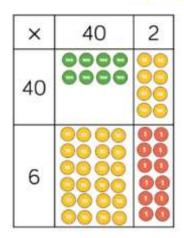
- Multiply multi-digit number up to 4 digits by a 2-digit number using the formal written method of long multiplication.
- Divide numbers up to 4 digits by a 2-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding as appropriate for the context.
- Divide numbers up to 4 digits by a 2-digit number using the formal written method of short division, interpreting remainders according to the context.
- Perform mental calculations, including with mixed operations and large numbers.
- Identify common factors, common multiples and prime numbers.

Concrete



Pictorial

Thousands	Hundreds	Tens	Ones
1000		00	000
		00	000
1000		00	000



Abstract

		4	2	1	6
X				3	4
	1	6	8	26	4
1	2	6	14	8	0
1	4	3	3	4	4
	1	1	1	F	F

_						_
			5	7	8	
1	5	8	6	7	0	
	-	7	5	ţ	Τ	
		1	1	7		
	-	1	0	5	ļ	
			1	2	0	

Key Vocabulary:

Multiplication Grouping Decimal Factors

Lots of Place Value Holder Remainder Prime Numbers

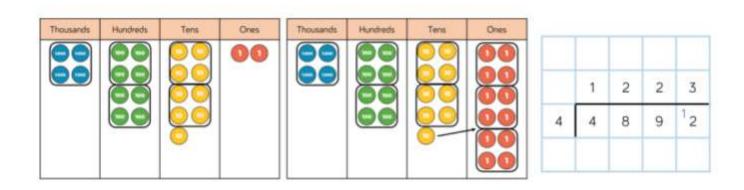
STEM Sentences:

What is important to remember as we begin multiplying by the tens number?

Why is the context of the question important when deciding how to round the remainders

Place in here any additional Knowledge you think appropriate in each element having reviewed the knowledge organiser for your year group for each of the strands of maths.

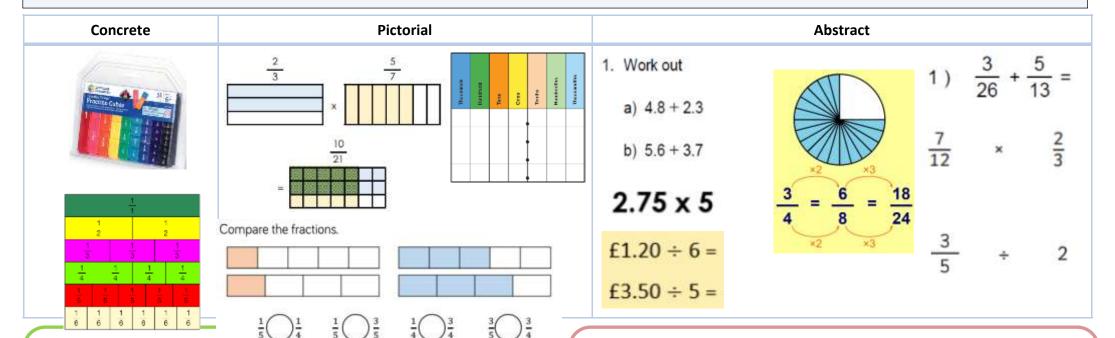
Additional pictorial representation of division:



Progression and Calculation Document — Fractions and Decimals Year Six

NC Learning Objectives:

- use common factors to simplify fractions; use common multiples to express fractions in the same denomination
- compare and order fractions, including fractions > 1
- add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
- multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $1/4 \times 1/2 = 1/8$]
- divide proper fractions by whole numbers [for example, $1/3 \div 2 = 1/6$]
- associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 3/8]
- identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places
- multiply one-digit numbers with up to two decimal places by whole numbers
- use written division methods in cases where the answer has up to two decimal places
- solve problems which require answers to be rounded to specified degrees of accuracy
- recall and use equivalences between simple fractions, decimals and percentages, including in different contexts



Key Vocabulary:

Division Subtraction Common Denominator Part **Equivalent Decimal Place** Multiplication Whole **Decimal Point** Place Value Denominator Fraction Addition Numerator Lots of Top Heavy **Mixed Number** Simplify

STEM Sentences:

How do I know if my answer is simplified fully?

Does multiplying two numbers always give you a larger product? Explain why.

Which equation has the largest answer? Can you order the answers to the equations in descending order?

Place in here any additional Knowledge you think appropriate in each element having reviewed the knowledge organiser for your year group for each of the strands of maths.

Simplify Fractions

We can use our knowledge of equivalent fractions to simplify fractions. To find the simplest form of a fraction, we divide the numerator and denominator by their highest common factor.

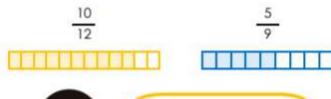
12 Factors of 12: 1, 2, 3, 4, <u>6</u>, 12 18 Factors of 18: 1, 2, 3, 6, 9, 18

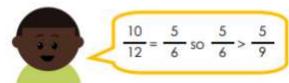


$$\frac{12}{18} \frac{+6}{+6} = \frac{2}{3}$$

Compare and Order Fractions

To **compare** and **order** fractions, we need to find a common denominator or numerator.





Find the Whole

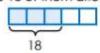
We can find the whole amount using the known value of a fraction.

To do this, we divide the known value by the numerator and multiply this by the denominator.



Jane ate $\frac{3}{5}$ of a box of strawberries.

She ate 18 of them altogether.

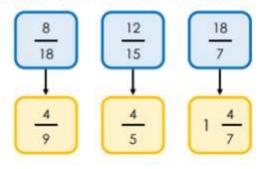


$$18 \div 3 = 6$$
 so $\frac{1}{5} = 6$

 $6 \times 5 = 30$ so the whole is 30

There were 30 strawberries in Jane's box.

These fractions have been ordered from smallest to greatest. Their equivalent fractions using common numerators are shown beneath,



Multiply Fractions by Fractions

To **multiply fractions by fractions**, we multiply the numerators together and multiply the denominators together.

$$\frac{2}{3} \times \frac{5}{7} = \frac{10}{21}$$

Divide Fractions by Integers

To divide fractions by integers, we divide the numerator by the whole number.

If the numerator is a multiple of the integer, then this is nice and simple!

$$\frac{6}{11} \div 3 = \frac{2}{11}$$

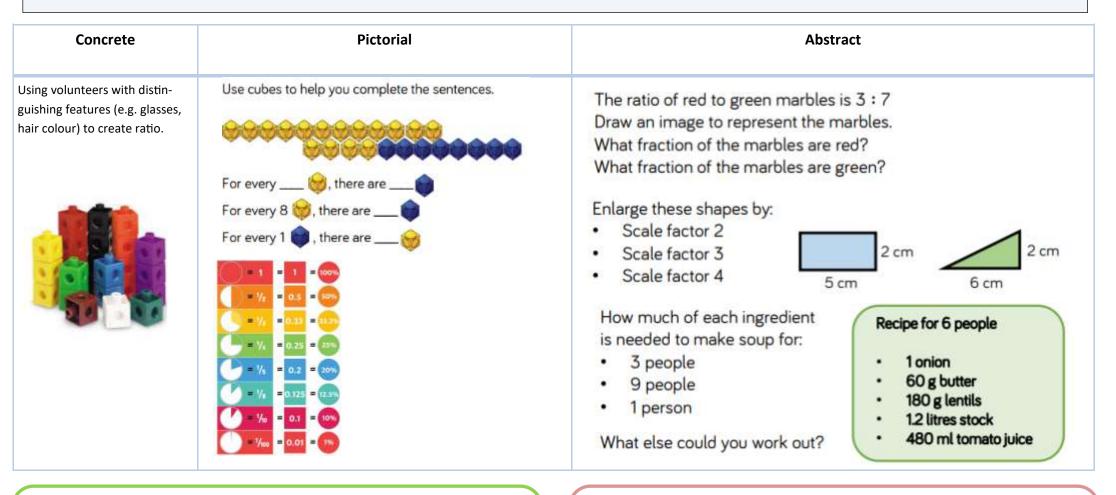
If the numerator is not a multiple of the integer, then we could use diagrams to help us.

$$\frac{3}{4} \div 2 = \frac{3}{8}$$

Progression and Calculation Document— Ratio and Proportion Year Six

NC Learning Objectives:

- solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts
- solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison
- solve problems involving similar shapes where the scale factor is known or can be found
- solve problems involving unequal sharing and grouping using knowledge of fractions and multiples.



Key Vocabulary:

Part of Blocks Ratio Proportion Percentage Scale Factor Amount of 10% Conversion 'Out of a whole' Bar Model Colon

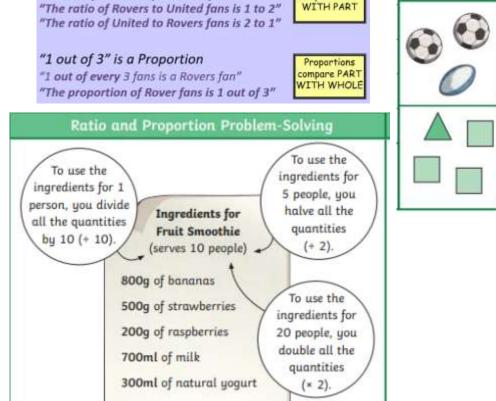
STEM Sentences:

What does the: symbol mean in the context of ratio?
Why do we have to double/triple all the sides of each shape?
Why is the order of the numbers important when we write ratios?
How would your sentence change if there were 2 more blue flowers?

"1 to every 2" is a Ratio

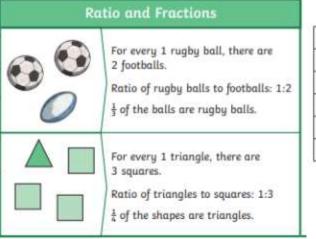
"1 Rovers fan to every 2 United fans"

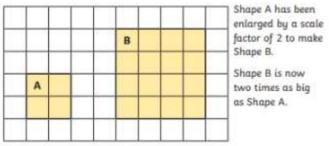
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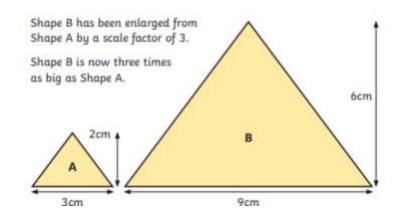


Ratios

compare PART







Progression and Calculation Document— Algebra Year Six

NC Learning Objectives:

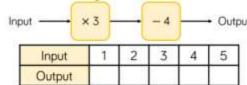
- use simple formulae

 generate and describe linear number sequences
- express missing number problems algebraically **1**
- find pairs of numbers that satisfy an equation with two unknowns
- enumerate possibilities of combinations of two variables.

Use items—such as cubes. 1 3 6 10 15 How is the sequence being generated? What is this sequence called? -5 -5 33 28 23 18 13 8 How many paperclips in the pot? 2 1 1 1 2 2 5

Abstract

Complete the table for the given function machine.



- · What patterns do you notice in the outputs?
- What is the input if 20 is the output? How did you work it out?

Substitute the following to work out the values of the expressions.

$$w = 3$$
 $x = 5$ $y = 2.5$

- w + 10
- w + x
- y w

Can you write a similar word problem to describe this equation?

$$74 = 15t + 2m$$

Key Vocabulary:

Terms Represent Constant Value Alphabet Letters Function Expression Equation Algebraic Solve Nth Term Sequence Pattern 'Collect Like Terms'

STEM Sentences:

What do you think 'one-step function' means?

If I change the order of the functions, is the output the same?

What does it mean when a number is next to a letter?

What tells you something is a formula?

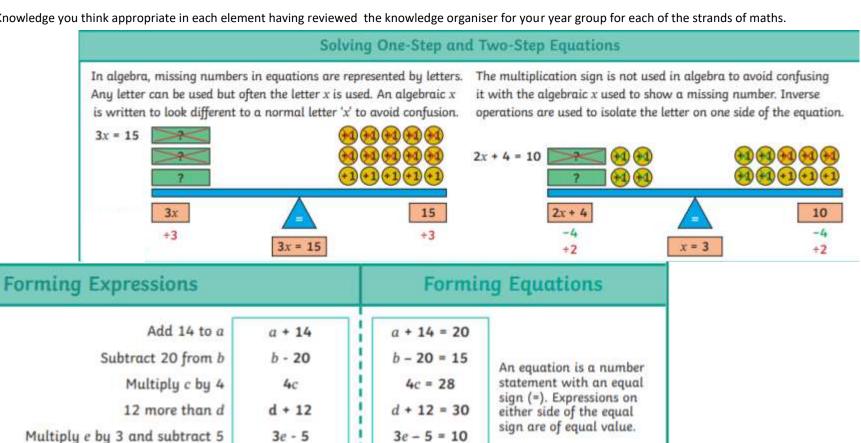
An expression is a group

of numbers, letters and

operation symbols.

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2(f + 12)



Formulas / Formulae

2(f + 12) = 44

(The word formula has two possible plural forms, formulae and formulas.)

Add 12 to f and then multiply by 2

A formula is a special type of equation that shows the relationship between different substituted variables. Formulas are often used in geometry to find area and volume.

Area of triangle = (base × height) + 2

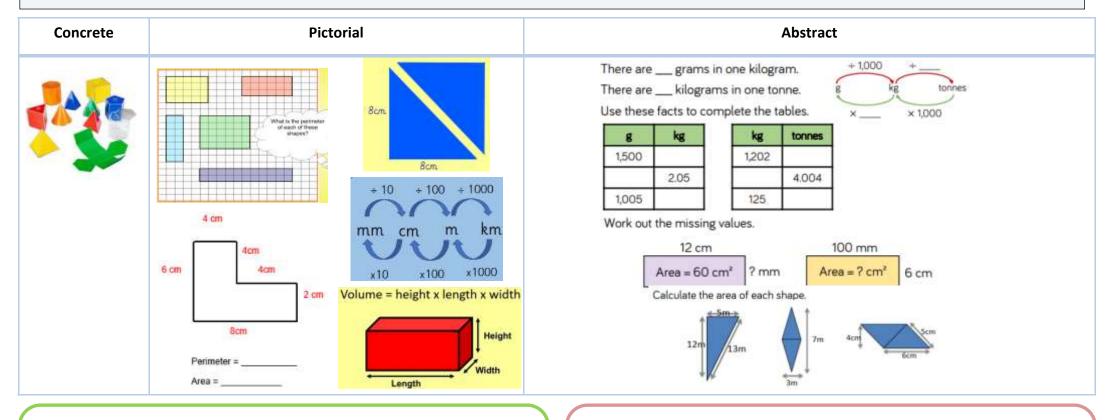
Area of rectangle = length x width

(12.5 × hours worked) + 25 = cost of job

Progression and Calculation Document — Measurement Year Six

NC Learning Objectives:

- solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate
- use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to three decimal places
- convert between miles and kilometres
- recognise that shapes with the same areas can have different perimeters and vice versa
- recognise when it is possible to use formulae for area and volume of shapes
- calculate the area of parallelograms and triangles
- calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) and cubic metres (m3), and extending to other units [for example, mm3 and km3].



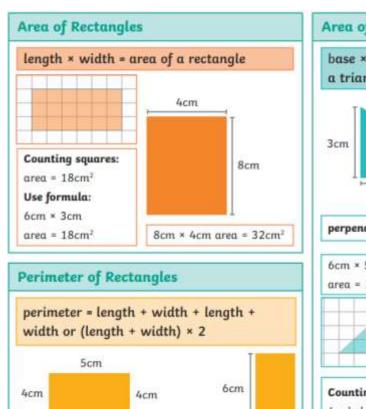
Key Vocabulary:

Cm m kg g l ml miles km mm tonnes measure units area perimeter Multiply cm^2 cm^3 3D shapes volume dimensions

STEM Sentences:

What is the difference between the area and perimeter of a shape? What is the same/different about the rectangle and triangle? What is the formula for working out the area of a rectangle or square? What do we mean by perpendicular height?

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2cm

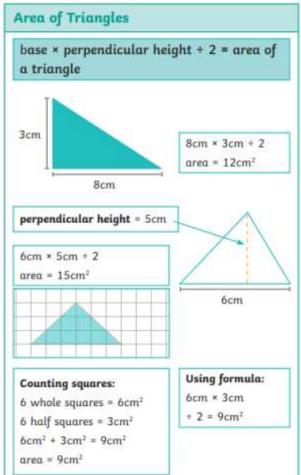
 $(6 + 2) \times 2$

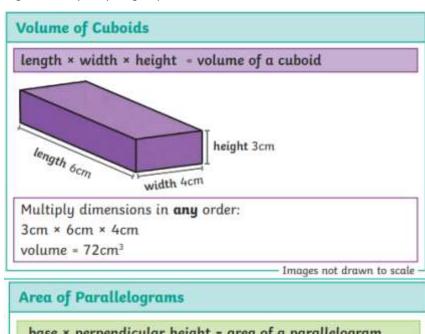
perimeter = 16cm

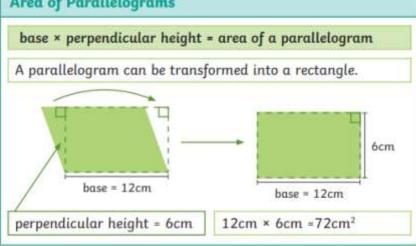
5cm

5cm + 4cm + 5cm + 4cm

perimeter = 18cm



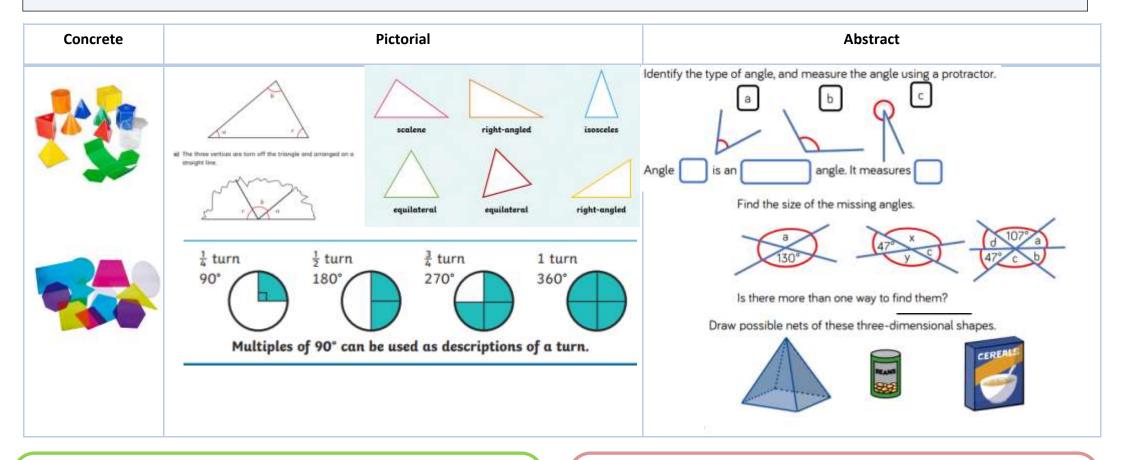




Progression and Calculation Document— Geometry Properties of Shapes Year Six

NC Learning Objectives:

- draw 2-D shapes using given dimensions and angles
- recognise, describe and build simple 3-D shapes, including making nets 🛽 compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons
- illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius
- recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles.



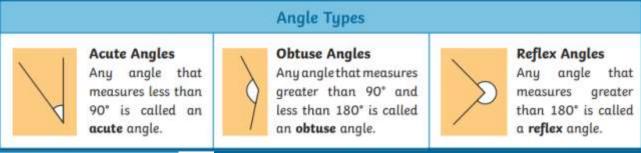
Key Vocabulary:

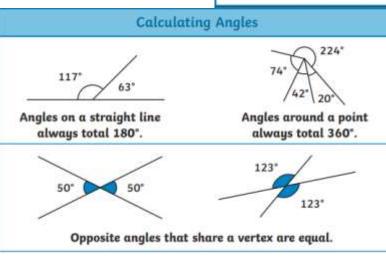
Angles Right Angle Acute Obtuse Reflex Area Perimeter Triangle
Right Angle Triangle Isosceles Triangle Scalene Triangle Circle Radius
Diameter Circumference Vertices Vertex Edges Faces

STEM Sentences:

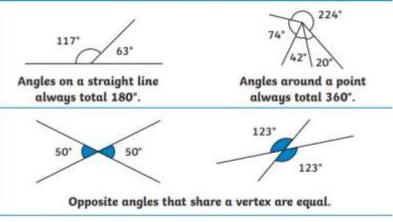
If we place two right angles together, what do we notice?
What is the most efficient way to calculate a missing angle?
Can you have an isosceles right angle triangle?
How can we work out the sum of the interior angles of a pentagon?

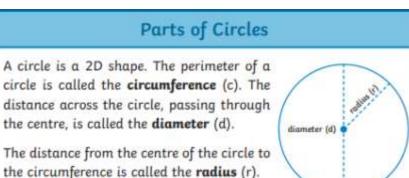
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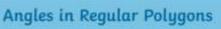


 $r \times 2 = d$

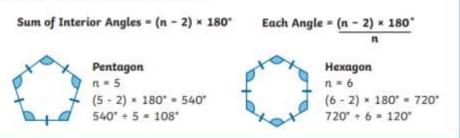




circumference (c)



As the number of sides of a polygon increases by one, the total of the interior angles increases by 180°. When n = number of sides, this formula can be used to find the size of each angle in a regular polygon:



Properties of 3D Shapes

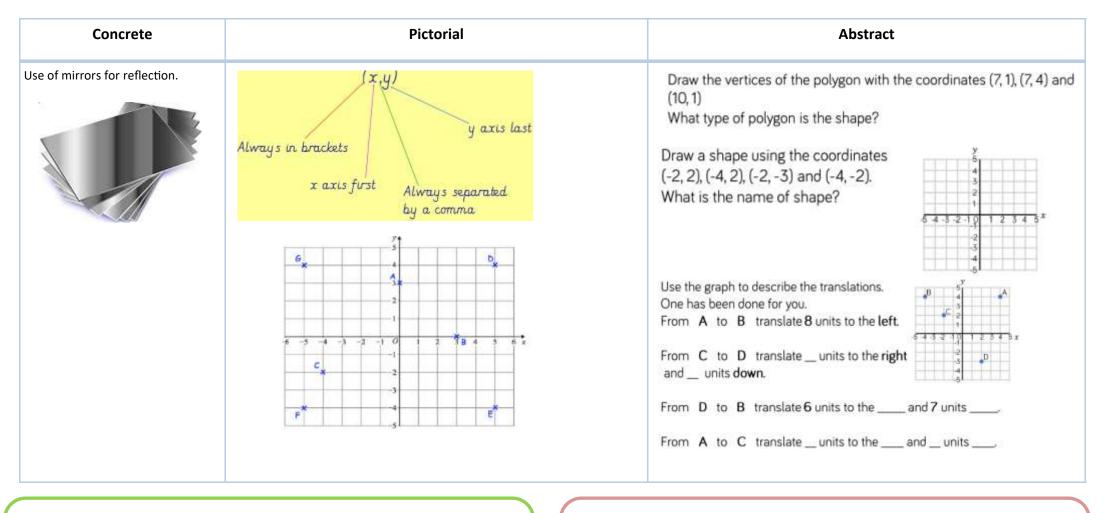
3D shapes have three dimensions - length, width and depth.

A polyhedron is a 3D shape with flat faces. Spheres, cylinders and cones are not polyhedrons as they have curved surfaces.

Cube	6 square faces 12 edges 8 vertices	Tetrahedron	4 triangular faces 6 edges 4 vertices	Sphere	1 curved surface 0 edges 0 vertices
Cuboid	6 faces 12 edges 8 vertices	Octahedron	8 faces 12 edges 6 vertices	Triangular p	orism 5 faces 9 edges 6 vertices
Square-based	pyramid 5 faces 8 edges 5 vertices	Cone	1 circular face 1 curved surface 1 curved edge 1 apex	Cylinder	2 circular faces 1 curved surface 2 curved edges 0 vertices

NC Learning Objectives:

- describe positions on the full coordinate grid (all four quadrants)
- draw and translate simple shapes on the coordinate plane, and reflect them in the axes.



Key Vocabulary:

X axis Y axis Coordinate Quadrant Positive Negative Brackets Comma Reflect Translate Transformation Rotate Scale Factor Enlargement Origin

STEM Sentences:

Can you draw a shape in the first quadrant and describe the coordinates?

Does each vertex translate in the same way?

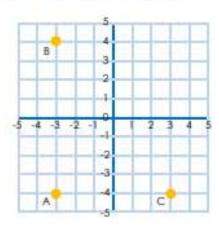
How is reflecting different to translating?

Which way do you move along the y axis and x axis to find negative numbers?

Place in here any additional Knowledge you think appropriate in each element having reviewed the knowledge organiser for your year group for each of the strands of maths.

Reflections

We can **reflect** points in the four quadrants by using the x or y axis as a mirror line.

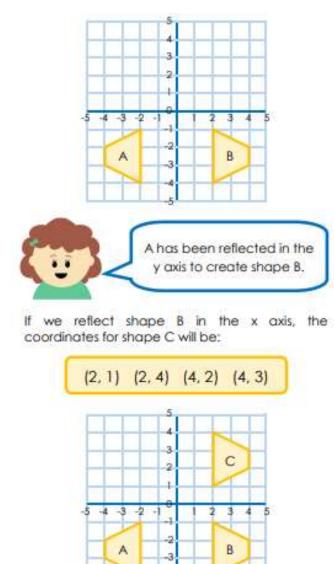




A has been reflected in the y axis to create point C.



As with translation, we can change the position of shapes on a grid by reflecting one coordinate at a time.



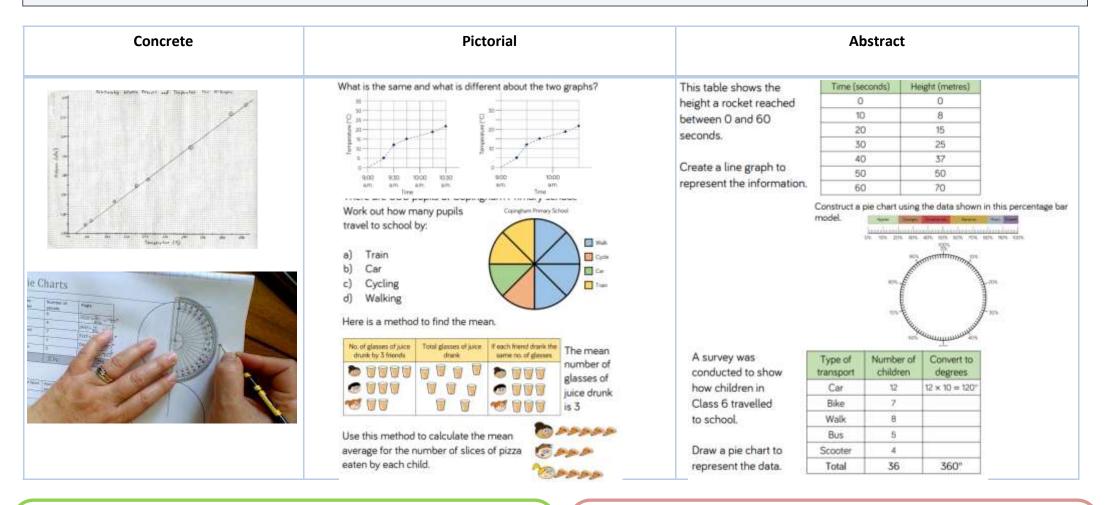
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Progression and Calculation Document — Statistics Year Six

NC Learning Objectives/Key Skills

- interpret and construct pie charts and line graphs and use these to solve problems
- calculate and interpret the mean as an average.



Key Vocabulary:

Mean Mode Median Range Average Line Graph Line of best fit

Pie Charts Percentage Axis Data Degrees

STEM Sentences:

Where might you see a line graph used in real life?

How will you make it clear which line represents which set of data?

What does the whole pie chart represent? What does each colour represent?

How many degrees are around a point? How will this help us construct a pie chart?

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